



DESIGN OF THE FUZZY CONTROL SYSTEM FOR THE WASTE HEAT UTILIZATION PLANTS DRIVEN BY THE THERMOACOUSTIC ENGINE

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Abstract: The paper addresses the synthesis of fuzzy controllers for computerized control system of the waste heat energy (WHE) utilization plants that operate with the thermoacoustic engine (TAE). Based on the analysis of existing systems, the authors present the main tasks of the synthesized control system, describe its structure and main components. Created system is then tested on the experimental thermoacoustic installation. Using the data obtained authors synthesize the mathematical model of thermoacoustic plant and describe the methodology of its control by the adjustments in resonator length of thermoacoustic device. Using the suggested approach authors design a number of conventional discrete and fuzzy controllers and provide the comparative analysis of quality indicators of the designed control systems transient responses. *Copyright © Research Institute for Intelligent Computer Systems, 2014. All rights reserved.*

Keywords: energy utilization, thermoacoustic plant, control system, fuzzy controllers

1. INTRODUCTION

The current state of society and industry leads to high energy consumption. High level of energy production causes the decrease in renewable mineral resources stocks and also the increase in global ecological problems, such as chemical pollution, thermal emissions and greenhouse gases. Therefore, the innovative energy efficiency technologies development and implementation is a primary task.

Today the thermal power plants (TPP), which operate through heat engines, provide most of energy. In simplified form energy balance of conditional TPP can be written as

$$Q_{fuel} = Q_{he} + Q_{wh} + Q_{loses} \quad (1)$$

Modern heat engines are able to convert only part of the fuel heat into mechanical energy Q_{he} . The work of heat engine is accompanied by the emission of heat in the environment $Q_{wh} + Q_{loses}$. Part of this emission that can be reused by existing TPP is the waste heat energy resources Q_{wh} . The heat that is technologically impossible or economically impractical to use creates the thermal pollution Q_{loses} .

The part of energy converted by the engine Q_{he} shows the degree of heat engine technical and

thermodynamic perfection. The value of Q_{wh} depends on the structural effectiveness, coolant temperature, TPP's thermo-physical properties, and existing technologies. Thus, applying the new saving technologies to increase the value of Q_{wh} in existing energy plants and systems is an important task.

Presently, there is a number of new technologies for energy utilization, among them the one based on thermoacoustic effect [1]. Thermoacoustics combines the fields of thermodynamics and acoustics and describes the process of interaction between heat and sound energy. The work of thermoacoustic devices (TAD) is based on the mutual transformation of heat and acoustic energies. The main feature of thermoacoustic systems is that unlike the other heat machines, the powerful acoustic pulses [2], generated by TAD are the carriers of mechanical energy and the "executive mechanism" of thermodynamic cycle.

Considering the thermoacoustic processes (TAP) reversibility, thermoacoustic devices can be divided into two main types [3-5]:

- thermoacoustic engines (TAE) that consume supplied heat energy and produce acoustic wave inside the resonator;
- thermoacoustic refrigerators (TAR) and heat pumps (TAHP) that consume energy from supplied

status of TAD peripheral equipment and sends it to PC through the Ethernet networks.

The designed system allows the communication between all components via RS232 network, also to enable the transfer of large amounts of data, PLC supports the Ethernet connection with PC and MCU can communicate with PC via USB. This grants maximum flexibility to designed distributed computer system.

Created software for PC allows storing the received from the controller information in the archive database; execution of the necessary algorithms for digital processing of measured signals, and displaying all available information on the user's screen.

Therefore, the proposed structure of distributed computer system allows the registration and ongoing monitoring of the thermoacoustic processes.

3. EXPERIMENTAL STUDIES OF THERMOACOUSTIC ENGINE

The tests of proposed by the authors computerized system were conducted using the experimental thermoacoustic engine (Fig. 2) [1,7], with a resonator length of 1010 mm and diameter of 46 mm, which was filled with air at atmospheric pressure. Engine was coupled with thermoacoustic heat pump (TAHP), which acted as a payload of the system (Fig. 1).

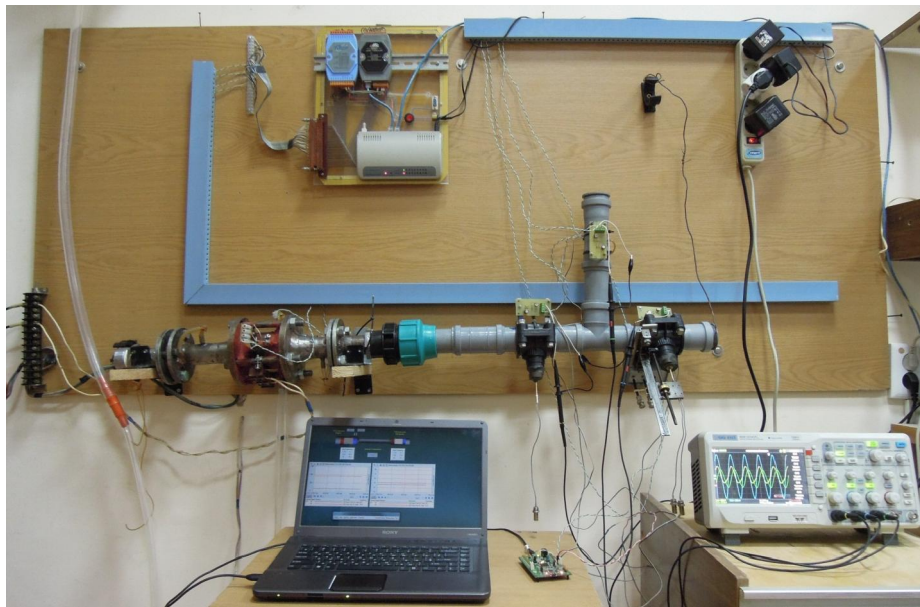


Fig. 2 – Photo of the experimental plant for TAD analysis

TAE convert's supplied heat P_Q into acoustic power P_{ac} , so its efficiency can be estimated as the ratio of established acoustic power to the supplied heat. In the experimental plant (Fig. 1) the nichrome heater is used as a source of the thermal energy P_Q and thus supplied power P_{supl} can be calculated through the consumption of electricity P_{el} by the heater (2), supplied by the power supply unit and measured by the current sensor ACS712ELCTR-05B-T, and the voltage divider.

$$\eta_{TAE} = \frac{P_{ac}}{P_{supl}} \cdot 100\% = \frac{P_{ac}}{P_{el}} \cdot 100\%, \quad (2)$$

To calculate the acoustic power P_{ac} , the information from two pressure sensors MPXV7007DP (PS1 and PS2 in Fig. 1), which are situated at a $\Delta x=160$ mm distance from each other, is collected by the MCU. Based on the data obtained from PS1 and PS2 the acoustic power can be

calculated using the two sensor method [6]. This method allows the calculation of pressure $p_0(t)$, particle velocity $v_0(t)$ and acoustic power $P_{ac}(t)$ at the point that is situated in the middle ($\Delta x/2$) between the points of pressure measurements. It should be noted that calculated by the described method values of particle velocity $v_0(t)$ and acoustic power P_{ac} were verified by the data obtained directly from the hot-wire anemometer.

Distance from the engine edge to the first pressure sensor is 745 mm, and to the second – 905 mm. Control of thermal data of the system was carried out using the thermocouples TS (Fig. 1).

Fig. 3 shows the results of TAE experimental measurements. Fig. 3, a illustrates the parameters of acoustic waves that were calculated using two sensors method. Thermoacoustic engine starting process is shown in Fig. 3, b, where on the top there are rooted mean square values (3) of calculated pressure $p_0(t)$ and particle velocity $v_0(t)$ and on the

bottom – temperature changes in points TS1 and TS2 (Fig. 1).

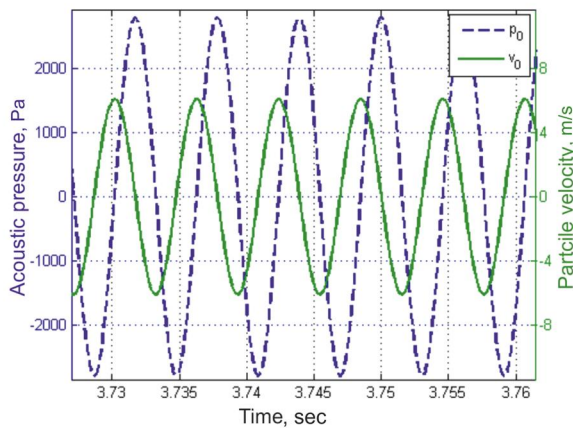
$$RMS(x) = \sqrt{\frac{1}{N} \sum_{k=1}^N x_k^2}, \quad (3)$$

where x_k – experimental data sample, $N=10000$ samples – RMS period.

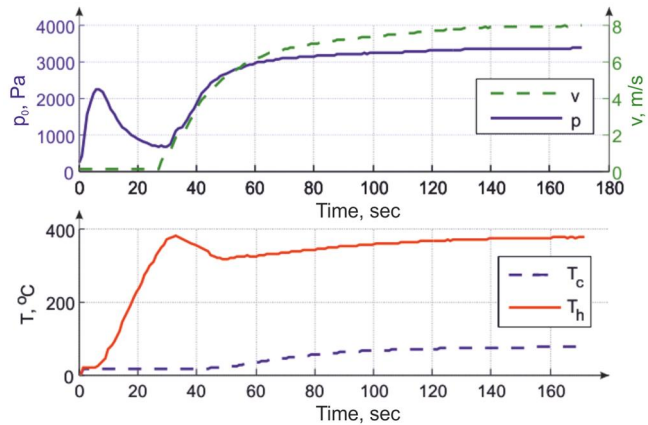
Calculated TAE efficiency values along with other experimental results are shown in Table 1. The experimental series include five tryouts with different supplied power. It should be noted that these values of efficiency are typical for air filled TAD working under atmospheric pressure.

Table 1. Results of the experimental study of TAD acoustic energy parameters

Parameter	Experiment number				
	1	2	3	4	5
T_H, K	548.6	568.5	632.5	594.9	648.6
T_C, K	287.8	303.8	320.1	322.5	349
I, A	2.3	3	3.5	4	5
U, V	23.1	31.1	37	41.5	51.8
P_{el}, W	53.13	93.3	129.5	166	259
p_0, Pa	543	1768	2021	2795	4128
$v_0, m/s$	0.85	3.2	3.8	5.93	7.27
P_{ak}, W	0.39	4.8	6.4	14.16	22.4
$\eta_{TAE}, \%$	0.73	5.14	5	8.53	8.56



a) instant values of pressure $p_0(t)$ and velocity $v_0(t)$



b) TAE starting process

Fig. 3 – Results of the experimental study of TAE working process

Enhancements of TAE efficiency can be achieved by the structural changes in the engine, increase of the operating pressure in the resonator and by replacement of the TAE working fluid from air to helium.

Further research showed that in given configuration the maximum pressure magnitude inside the TAE resonator depends on the length of TAHP resonator branch [7]. Thus, the control of TAD working process can be made by the adjustments in TAHP resonator length. Therefore, further let's consider the synthesis of TAD control system based on the change of the TAHP resonator length.

4. SYNTHESIS OF THE THERMOACOUSTIC PROCESSES CONTROL SYSTEM

Based on the results of experimental studies (Fig. 3), it can be concluded that the TAE can be described by the first order transfer functions that represent the pressure $p(t)$ and particle velocity $v(t)$ which are generated due to the supplied power $P_{supl}(t)$. The exact values of pressure (4) and

velocity (5) transfer functions (TF) were identified using the least squares regression method [8] with the desired functionality in the form (6).

$$W_p(p) = \frac{14.66}{48.72 p + 1}, \quad (4)$$

$$W_U(p) = \frac{5 \cdot 10^{-5}}{41.36 p + 1}, \quad (5)$$

It should be noted that TF $W_U(p)$ (5) represents volume velocity in TAE resonator and it can be calculated as $U(t)=v(t)A$ with A is the cross section area of TAE resonator.

$$\min_{k,T} J(k, T) = \min_{k,T} \sum_{j=1}^N \left[\frac{k}{T} e^{-\frac{t}{T}} - y_j \right]^2, \quad (6)$$

where k, T – parameters of first order link, y – experimental sample, N – experimental sample length.

TAHP branch is represented by the transfer matrix $W_{TAHP}(p)$ that is based on the Rott's

representation of continuity (7) and momentum (8) equations [1] and identified model (9) of temperature difference $W_T(p)$ between the stack hot TS4 and cold TS3 ends (Fig. 1). For the given geometry of experimental thermoacoustic plant equations (7) and (8) can be represented by a matrix (10).

The change of the TAHP resonator length is simulated by the system that transforms direct

$$\frac{dp}{dx} = -\frac{1}{A} \frac{i\omega\rho_m}{1-f_v} u_1, \tag{7}$$

$$\frac{du_1}{dx} = -A \frac{i\omega[1+(\gamma-1)f_k]}{\gamma p_m} p + \frac{f_k - f_v}{(1-f_v)(1-\sigma)} \frac{1}{T_m} \frac{dT_m}{dx} u_1, \tag{8}$$

$$W_T(p) = \frac{7,18 \cdot 10^{-4} p + 6,05 \cdot 10^{-6}}{p^2 + 0,12 p + 5,49 \cdot 10^{-4}}, \tag{9}$$

$$W_{TATH}(p) = \begin{bmatrix} 0.903 + 0.002i & 1.006 \cdot 10^3 + 9.094 \cdot 10^4 i \\ -9.715 \cdot 10^{-9} - 2.024 \cdot 10^{-6} i & 0.903 + 0.002i \end{bmatrix}, \tag{10}$$

where ρ_m – density of the medium; σ – Prandtl number; T_m – function of the temperature field distribution along the resonator; p – acoustic pressure; u_1 – volume velocity; f_v та f_k – Rott functions that depend on the geometry and thermal properties of the stack and gas mixture; γ – universal gas constant, for air $\gamma=1.4$; A – cross sectional area of resonator; i – imaginary unit; ω – acoustic wave frequency.

$$f_{res} = \frac{a}{\lambda} = \frac{\sqrt{\gamma k T / m}}{nL}, \tag{11}$$

where f – sound wave frequency; a – speed of sound; λ – sound wave length; k – Boltzmann constant; γ – the adiabatic coefficient of gases; T – absolute temperature; m – molecular mass of gas; L – resonator length; n – acoustic wave length multiplier.

The resulting linear [9] model of TAD is shown in Fig. 4. The input values for the system are: supplied to TAE electric power P_{supl} , starting length of TAHP resonator L_{TAHP} , value of cold end of TAHP stack T_C , value of speed of sound $a=343$ m/s and desired temperature T_{des} of TAHP stack hot end.

The acoustic wave length multiplier n , for current setup is equal to 2 (half wave length resonator), k_R is the reduction gear coefficient that transforms rotational movement of the DC engine into the TAHP resonator end piston translational movement.

current (DC) engine $W_{DCE}(p)$ rotational movement into linear using the reduction gear. The effect of resonator length change is simulated by the experimentally obtained nonlinear dependency of pressure magnitude $p(t)$ from the acoustic wave frequency inside the TAHP resonator.

The relation between TAHP resonator length L_{res} and acoustic wave frequency f_{res} are caharacterized by equation (11).

The acoustic pressure magnitude is adjusted by the value of the nonlinear dependency $p_m(f_{res})$, which is normalized by the pressure value at the resonant frequency (11). The output of the system is the value of the TAHP stack hot end $T_H(p)$.

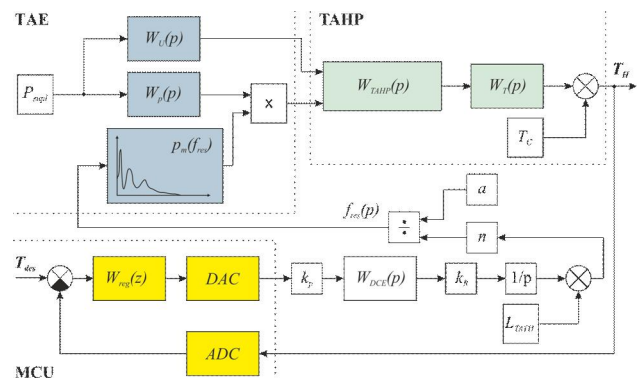


Fig. 4 – The resulting model of the system for TAD control by the TAHP resonator length adjustment

The simulation of synthesized TAD model working process is shown in Fig. 5.

It demonstrates that the implementation of control system decreases the transient response time (with 5% setting bounds) from $t_{trans}^{TAD} = 365.6$ sec to

$$t_{trans}^{PD} = 301.3 \text{ sec.}$$

The desired value of TAHP stack hot end is set to $T_{des}=45$ °C. Synthesized system uses the discrete [10] proportional-derivative (PD) regulator, whose transfer function is defined in the equation (10).

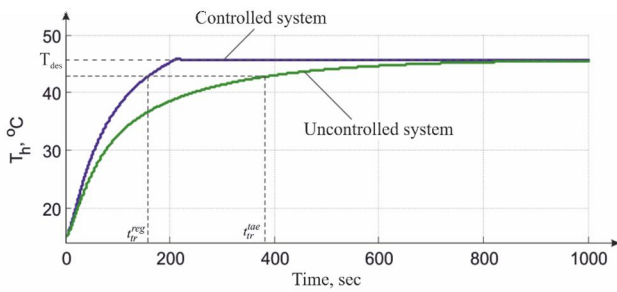


Fig. 5 – Simulation results of synthesized TAD model

$$W_{reg}(z) \Big|_{T_0=0.1} = \frac{6.037z - 5.374}{z - 0.06542} \quad (12)$$

It should be noted that the discretization period of $T_0=0.1$ sec is equal to the sample time of thermocouple data acquisition module.

5. SYNTHESIS OF FUZZY CONTROLLERS FOR THE TAE DRIVEN PLANT

Fuzzy control provides a formal methodology [11] for representing, manipulating, and implementing a human’s heuristic knowledge about how to control a system.

Fuzzy controllers are applicable primarily to manage objects that either could not be described or could be described with great difficulties. However, even for control objects, for which mathematical model could be obtained, these regulators are often better than others, because they allow to obtain higher quality (fewer errors in transient and steady state) of automatic control.

The microcontroller based fuzzy controller [12] block diagram for thermoacoustic plant is given in Fig. 6, where the fuzzy controller embedded in a closed-loop control system is shown.

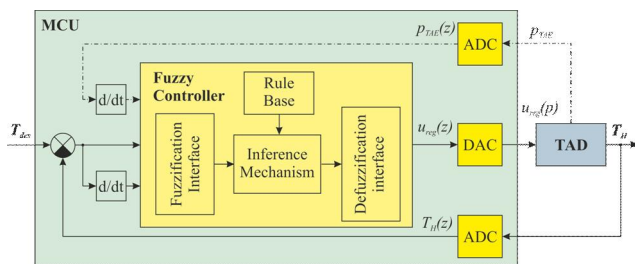


Fig. 6 – Block diagram of the TAD control system with MCU-based fuzzy controller

Authors designed [13] PD fuzzy controllers of Mamdani and Sugeno types for the control system of thermoacoustic plant. The input signals for controllers are the error signal between the desired and current temperature of hot end of TAHP stack ($\varepsilon = T_{des} - T_H$) and the first derivative of the error signal. Input signals of fuzzy controllers are

described by five triangular terms, and the output signal u_{reg} is described by the seven terms for Mamdani controller (Table 2) and first order polynomial for Sugeno controller. The knowledge base of fuzzy system consists of 25 rules (Table 3).

Table 2. Terms of Mamdani fuzzy controller

Term	Membership function	Range of values
For input variable ε		
BN – Big Negative	Triangle	[-1.5 -1 -0.5]
SN – Small Negative	Triangle	[-1 -0.5 0]
Z – Zero	Triangle	[-0.5 0 0.5]
SP – Small Positive	Triangle	[0 0.5 1]
BP – Big Positive	Triangle	[0.5 1 1.5]
For input variable $d\varepsilon/dt$		
BN – Big Negative	Triangle	[-1.5 -1 -0.5]
SN – Small Negative	Triangle	[-1 -0.5 0]
Z – Zero	Triangle	[-0.5 0 0.5]
SP – Small Positive	Triangle	[0 0.5 1]
BP – Big Positive	Triangle	[0.5 1 1.5]
For output variable u_{reg}		
BN – Big Negative	Triangle	[-1.5 -1 -0.67]
MN – Middle Negative	Triangle	[-1 -0.67 -0.33]
SN – Small Negative	Triangle	[-0.67 -0.33 0]
Z – Zero	Triangle	[-0.33 0 0.33]
SP – Small Positive	Triangle	[0 0.33 0.67]
MP – Middle Positive	Triangle	[0.33 0.67 1]
BP – Big Positive	Triangle	[0.67 1 1.5]

Table 3. Knowledge base of Mamdani fuzzy controller

		Error derivative, $d\varepsilon/dt$				
		BN	SN	Z	SP	BP
Error, ε	BN	BN	BN	BN	MN	SN
	SN	BN	MN	MN	SN	SP
	Z	SN	SN	Z	SP	SP
	SP	SN	SP	MP	MP	BP
	BP	SP	MP	BP	BP	BP

Transient responses comparison of created Mamdani and Sugeno fuzzy controllers with two input variables is given in Fig. 7. Based on the analysis of results obtained (Fig. 7) it could be concluded that the Sugeno fuzzy controller enhances the control system with best quality indicators of transient response, including the response time of 149.39 sec and static error of 0.06°C.

Application of fuzzy logic paradigms [13,14] for design of controllers for WHE utilization system driven by the TAE allows to create the hybrid controller that responds not only to changes in the values of the hot heat exchanger of TAHP branch (T_H), but also to the value of the pressure derivative (p_{TAE}) inside the TAE. Additional feedback is shown in Fig. 6 by the dash-dot line. Synthesized according to this principle hybrid Sugeno fuzzy controller has three input signals, each of which is described by

five triangular terms and their relations are characterized by the knowledge base, consisting of 125 rules. Seven first order polynomials form the output signal of the controller.

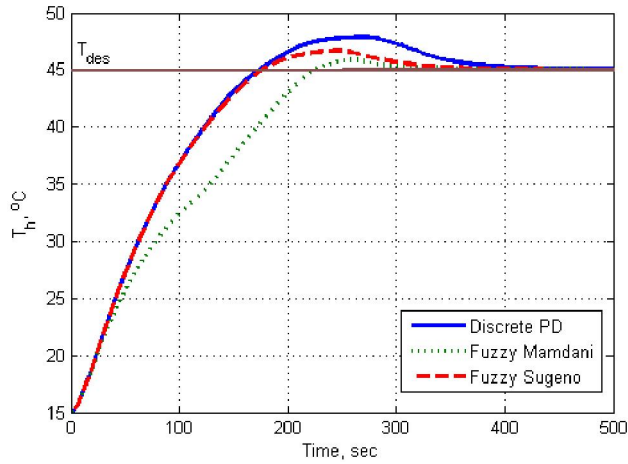


Fig. 7 – Comparison of designed fuzzy and discrete PD controllers

Input membership functions of the hybrid fuzzy controller are given in Fig. 8 and its characteristic surfaces are shown in Fig. 9. A comparative analysis of the quality indicators of the TAD control system transient response (Fig. 10) with PD and hybrid Sugeno fuzzy controllers are shown in Table 4.

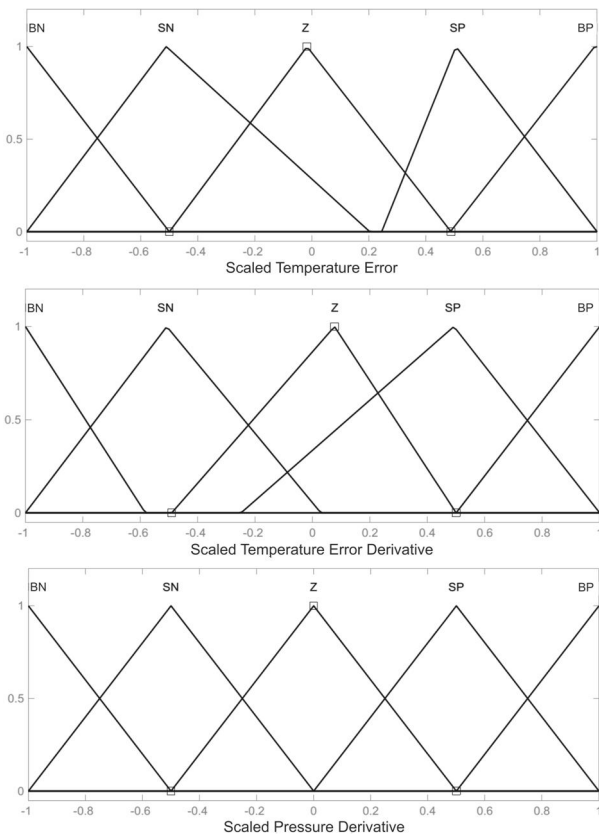
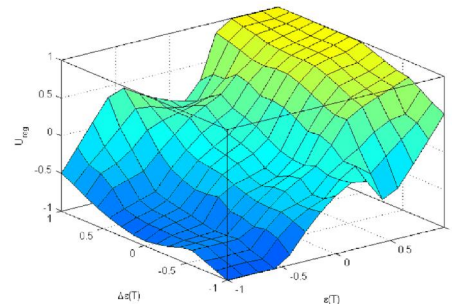
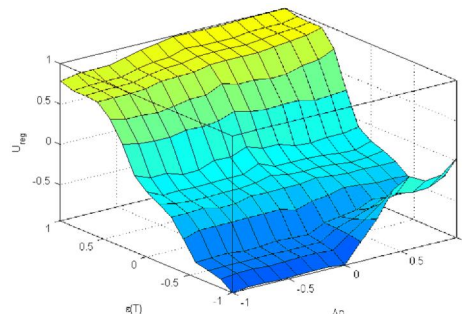


Fig. 8 – Input membership functions of the synthesized hybrid fuzzy controller

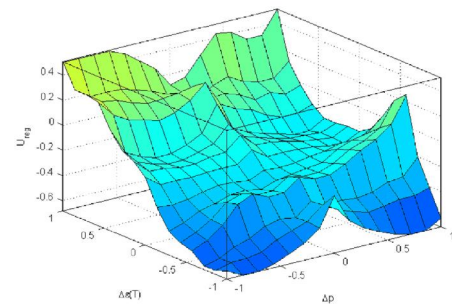
Designed hybrid fuzzy controller provides better dynamical characteristics of the WHE utilization system driven by the thermoacoustic engine. It should be noted that with the introduction of an additional variable to the regulating law it is possible to increase the robust properties of the synthesized control system.



a) $u_{reg} = f(d\varepsilon, \varepsilon)$



b) $u_{reg} = f(\varepsilon, dp)$



c) $u_{reg} = f(d\varepsilon, dp)$

Fig. 9 – Characteristic surfaces of the synthesized hybrid fuzzy controller

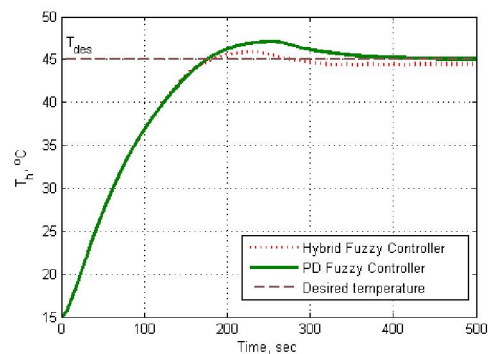


Fig. 10 – Comparison of designed PD and hybrid Sugeno fuzzy controllers

Table 4. Results of the experimental study of TAD acoustic energy parameters

Parameter	Discrete PD	Fuzzy Mamdani	Fuzzy Sugeno	Hybrid Sugeno
Transient response time, sec	301.3	197.65	149.39	146.77
Overshot, %	6.34%	1.97%	3.77%	1.97%
Static error, °C	0.06	0.03	0.06	0,56

6. CONCLUSION

The article presents the design of optimum controller for waste heat utilization plant with thermoacoustic engine. Authors describe the series of regulators that by changing the length of the heat pump branch resonator can stabilize the output temperature of the thermoacoustic system. A comparative analysis of continuous PD controller with the fuzzy controllers of Mamdani and Sugeno types showed the feasibility of control devices on fuzzy logic for control of thermoacoustic devices.

The authors propose a hybrid fuzzy logic controller which also reacts to changes in the acoustic pressure of the thermoacoustic engine. Such controller grants to the control system best dynamic qualities in comparison to other regulators (Table 4).

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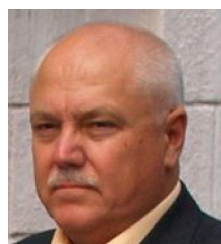
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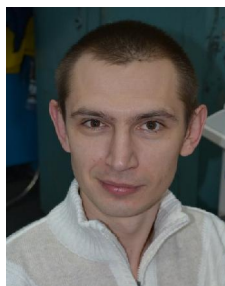
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